## Binomial Random Variable

$$P(\chi) = \binom{n}{\chi} p^{\chi} q^{n-\chi} , \quad \chi = 0,1,2,\dots, n$$

X. is a binomial random variable that represent the no. of sis in n-trials.

No. of trials | success!

D: probability of success in a single-trial

9: 1-P: probability of fail

Ex:

In an Experiment 10% of people passes. Suppose that 4 persons are selected at a random

(1) find the probability that none of the four persons passes

the test b) find the probability that three of the four parsons passes derive a formula for p(x), the probability distribution in of the binomial Prariable &

Solution.

none passer p(FFFF) \*  $p(x) = {}^{n}C_{x} p^{x} q^{n-x}$ 

at  $\chi = 0$  , n = 0 , p = 0.1 , 9 = 0.9

a)  $p(0) = 4c_0 (0.1)^0 (0.9)^{4-0} = (0.9)^4 #$ 

b)  $p(3) = {}^{4}C_{3} (0.1)^{3} (0.9)^{4-3} = 4(0.1)^{3} (0.9) \#$ 

 $\subset$ 

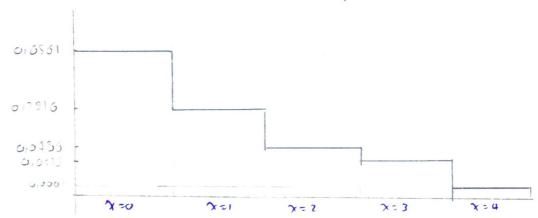
					T
$\gamma$	0	1	2	3	4
P(x)	0,6581	0,2916	010 486	0.00 30	0.0001

P(0)=

$$P(x) = {}^{n}C_{x} p^{x} q^{n-x}$$

$$P(0) = 0.6561$$

$$p(0) = 0.6561$$
  $p(1) = {}^{4}C_{1}(0.1)^{1}(0.9)^{3} = 0.2916$ 



$$M = np$$

Sheet 5

3) prove that for any random variable x

i) 
$$E(ax+b) = a E(x) + b$$

$$E(ax+b) = \int_{-\infty}^{\infty} (ax+b) p(x) dx = a \int_{-\infty}^{\infty} x p(x) dx + b \int_{-\infty}^{\infty} p(x) dx$$

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$$E(ax+b) = aE(x)+b$$

Give a formula for p(x) for a binomial random variable with n=7 and P=0.2

Solution ..

$$P(x) = \begin{pmatrix} 7 \\ x \end{pmatrix} (0.2)^{x} (1-0.2)^{7-x}$$

$$P(x) = \begin{pmatrix} 7 \\ x \end{pmatrix} (0.2)^{x} (0.8)^{7-x}$$

b) Consider the following 
$$V(x) = (\frac{5}{2}) (0.7)^{x} (0.3)^{5-x}$$
 .  $x = 0.1,2,3,4,5$ 

a) 
$$n = ?$$
 , b)  $p = ?$   
c) graph  $p(x)$   
d) find  $M$ ,  $Q^2$ ,  $Q$ 

Solution :

$$n = 5$$
,  $p = 0.7$ ,  $9 = 0.3$ 

~	0	1	7	3	4	5
ν(x)						

$$M = NP = 5 \times 0.7 = 3.3$$
  
 $Var = NP9 = 5 \times 0.7 \times 0.3 = 5$   
 $SD : \sqrt{Var} = 5$ 

(1) A fair coin \_\_\_\_\_ 6 times . head \_\_\_\_ success

find

() nra ha holidu Mat pradly Q heads account

() pro be bility that exactly 2 heads occur

(i) probability that at least theads

(ii) probability that no heads

(v) probability that at least one head.

Solution.

 $p(z) = {26 \choose 1} (0.5)^2 (0.5)^4 =$ 

(() 
$$N = 4, 9, 6$$
  
 $P(4,6,0.5) + P(-5,6,0.5) + P(6,6,0.5) =$